

# SIGNIFICANTLY-DIFFERENT WORD SQUARES

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In a May 1993 **Word Ways** article, Donald Knuth says that the reason his computer found so many 5x5x5 word cubes is that so many five-letter words can be "tweaked" into others. Each tweak or combination of tweaks can produce a new cube, only slightly different from the old one. All of us who have been finding word squares understand. The large numbers reported by Chris Long in the February 1993 **Word Ways** reflects this. To eliminate the effect of tweaking along the major diagonal (where a tweak always produces a new square), I devised the following procedure. I have been thinking about this for some time in regard to speeding the search for word squares; it can be applied to cubes equally well.

To start, my computer used 4839 common five-letter words to find 178,415 squares in 5.0 minutes. I then used a Carrollian ladder program to create a Boolean catalog. A number, BOO(x), was assigned to each word typically as follows. I illustrate with a subject word, CARES. BARES joins CARES in position 1; since B comes before C in the alphabet, mark BOO(CARES) in position 1. CORES joins CARES in position 2, but since O does not come before A, do not mark BOO(CARES). There are several words that mark BOO(CARES) in position 3. CARDS marks position 4, and CARED marks position 5. CARES ends up with a BOO of 10111 (decimal 23), CORES and CURES are similarly scored 31. BARED gets scored 4, being marked only by BAKED, which is scored 0.

In the second round, the computer ran all 4,839 words through a program which when looking for the nth word said if BOO(x) has a 1 in the nth position, do not use word x here. This program found 40,888 squares in only 2.3 minutes. Here are six squares sampled from forty (every thousandth square was printed out). Note that LEASE can be tweaked to LEAST in the first square, but the latter would not have been allowed. ASTER was allowed in the third square because neither ASKER nor ASPER were included in the basic list.

CAMEL	DRIPS	KVASS	MUFTI	SOAPS	VILLA
AGAVE	RADIO	VISIT	UHLAN	ONION	IDEAL
MAFIA	IDEAL	ASTER	FLASK	AISLE	LEANT
EVILS	PIANO	SIEGE	TASTE	POLKA	LANCE
LEASE	SOLON	STREP	INKED	SNEAK	ALTER

And then, for the sake of variety, I required the program to use five new words for each new square (in addition to the BOO test). I only got 225 squares this way; here are the last ones found.

SCUFF SIGMA SPRAT SPURT STRAW YACHT  
 COPRA INNER PLAZA PUREE TRIPE ARRAY  
 UPSET GNATS RADIX URBAN RIGID CROOK  
 FREES METRO AZIDE REACT APING HAOLE  
 FATSO ARSON TAXED TENTH WEDGE TYKES

For readers who are not familiar with computer logic, the word Boolean refers to the fact that my programs use Boolean AND/OR logic to mark and test the words.

Having catalogued the five-letter words, I decided to see what happens with cubes. Before proceeding, I reduced my list to 4712 words by eliminating a few that didn't seem to be common enough. It was not difficult to expand a computer program for squares into one for cubes; the resultant worked fine. Using the BOO logic described above, it found 243 cubes in a little more than three hours. Without the BOO, it might have found a thousand or so, in a much longer time.

Before presenting a few findings, let me describe the architecture of a cube. A 5x5x5 cube contains fifteen different words. When we describe the cube in the following manner, ten of the fifteen words are printed twice (not used twice). Letters along the main diagonal are in boldface. These are the ones to which the BOO logic was applied.

WORD 1	WORD 2	WORD 3	WORD 4	WORD 5
WORD 2	<b>WORD 6</b>	WORD 7	WORD 8	WORD 9
WORD 3	WORD 7	<b>WORD 10</b>	WORD 11	WORD 12
WORD 4	WORD 8	WORD 11	<b>WORD 13</b>	WORD 14
WORD 5	WORD 9	WORD 12	WORD 14	<b>WORD 15</b>

Here are some cubes (asterisks indicate tweakable letters):

*		*		*		*		*		*				
abbot	beach	baste	octet	theta	<b>eagle</b>	aglow	clove	hewer	slope	toyer	ewers	evens	terse	arses
balsa	<b>anahs</b>	lapis	shite	asset	moron	arena	honor	<b>snare</b>	pedal	inane	sales	tonic	erect	tests
cable	ables	blcat	leave	ester	<b>bleat</b>	lento	eaten	stone	<b>onion</b>	atone	toned	venam	<b>enery</b>	redye
dodge	dboes	doses	geese	esses	bruin	cutdo	eider	snort	steel	<b>edera</b>	solar	semis	erase	strep
<b>ennui</b>	nears	<b>nasal</b>	urate	isled	eclat	alive	raven	steno	siren	avert	lento	terse	enter	doors
fiche	isles	cleat	heave	ester	<b>sweat</b>	lento	eaten	stone	<b>endow</b>	atone	towel	venam	<b>enera</b>	relax
grade	rubes	about	deuce	ester	usurp	burro	error	<b>spore</b>	orbit	urine	totes	conic	erect	rests
heaps	eclat	alone	<b>panda</b>	stead	chive	liras	avail	tesla	orbit	naive	ester	diver	alert	darts
japan	alamo	pavid	amide	nodes	lilac	alone	mania	<b>ocean</b>	vowel	inert	delta	dirge	<b>eater</b>	snare
kaput	arass	<b>pasha</b>	usher	tsars	mulct	altar	scale	strep	stave	haven	arena	elect	rents	spasm
legit	<b>evade</b>	gales	ideal	tesla	vigas	agent	dance	ester	levee	<b>enera</b>	steam	acmes	lease	armed

These cubes use commoner words than those of Donald Knuth, and they don't contain his flaw of using a word twice. Based on simple probability arguments, we do not expect a word to be chosen twice but the nature of the system makes it happen often enough. The computer program used here contains specific logic to prevent duplications. This is usually not necessary for squares.